

A P E N D I C E S

APPENDIX - A

Proof to show that elastic contact zone is zero for the case of chip-streaming when there is no workhardening

For chip-streaming case, first slipline field (Fig. 4.1(a)) is reduced to slip-line field model as given by Lee and Shaffer [12] (Fig.1.3). Angle made by α - line at DE is given by $\xi = 1/2 \cos^{-1} (m)$, where m is constant friction factor. Because of strain-hardening, the hydrostatic pressure (p_1) and the yield shear stress (k_1) on the tool face become different from those (p, k) on the slipline AC. Let $p_1 = m_1 p$ and $k_1 = m_1 k$, where m_1 is strain - hardening factor. Assuming power-law distribution of normal stress in the elastic zone, equilibrium of forces normal and along the chip-tool interface and moment about tool-tip yield following equations as follows :

$$(p' \sin \xi + \cos \xi) = m_1 (p' + \sin 2\xi) (1 + x/n + 1) \quad (A.1)$$

$$pa \cos \xi - ka \sin \xi = k \cos 2\xi b + k \cdot \cos 2\xi \cdot xb/n + 1 \quad (A.2)$$

$$p'/2 = m_1 (p' + \sin 2\xi) [y^2/2 + y^2 x(1+x)/n + 1 - x^2 y^2/n + 2] \quad (A.3)$$

where $Y = b/a$, $p' = p/k$ and $X = l_c/b$

These equations are solved for unknown parameters y , p' and X to give :

$$y = 1 / (m_1 (1 + X / n + 1) (\cos \xi + \sin \xi))$$

$$p' = 1$$

$$X^2 [m_1 (n + 2) - 2(n + 1)] + X [2m_1 (n + 1)(n + 2) - 2(n + 1)(n + 2)] +$$

$$[m_1 (n + 1)^2 (n + 2) - (n + 1)^2 - (n + 1)^2 (n + 2)] = 0.0 \quad (A.4)$$

The above quadratic equation may be solved to determine the value of X . It may be noted that X becomes equal to zero, when $m_1 = 1$. This indicates that there is no elastic contact for the case of chip-streaming, when there is no strain hardening of work-piece material.



APPENDIX B

Derivation of chip curl radius R_{chip} and moment arm

In fig. 7B.1 the plastic contact length l_p , the width of the chip-breaker W and the height of the chip-breaker h are indicated. The length of the chord EF is denoted as x . Now from triangle EGF , it is obtained

$$x = ((W - l_p)^2 + h^2)^{1/2}$$

The angle made by the chord with tool face at point E is denoted by θ . The value of θ is determined from the geometry of chip-breaker and slipline field as follows:

$$\tan\theta = h / (W - l_p)$$

A normal is drawn on tool face at point E which intersects the line of action of chip-breaking force at point O , which is the center of curvature of chip. Referring to triangle OEF , it is easily seen that the angle OEF and angle OFE are both equal to $\pi / 2 - \theta$. Using sine law the following relationship is obtained:

$$R_{\text{chip}} / \cos\theta = x / \sin 2\theta$$

$$\text{Hence, } R_{\text{chip}} = x / 2 \sin\theta$$

$$\text{But } \sin\theta = h / x$$

$$\text{Hence, } R_{\text{chip}} = x^2 / 2h = (W - l_p)^2 / 2h + h / 2$$

To determine the values of d (the perpendicular distance from point B in the slipline field to the line of action of the force F_b , a normal CQ is drawn on line FO from point C (tool tip). Similarly another normal is drawn on CQ at point P from point E and a

second normal is drawn on PE at point S from O. It is easily seen that the angles CEP and OES are equal to $\pi / 2 - 2\theta$ and 2θ respectively.

$$\text{Now, } CQ = PQ + PC = OS + PC = R_{\text{chip}} \sin 2\theta + l_p \cos 2\theta$$

$$\text{But } d = CQ - CI$$

BH and CH are the horizontal and the vertical distance of point B from C which are calculated from the slipline field and are denoted by H_{BC} and V_{BC} respectively. From point B a normal is drawn on CQ at point I and from point H two normals are drawn on BI and CQ at point M and N respectively.

It is easily seen that the angle PCH and the angle MBH are each equal to $2\theta - \gamma_0$.

$$CI = CN + NI = CN + MH = HC \cos(2\theta - \gamma_0) + BH \sin(2\theta - \gamma_0)$$

$$\text{Hence, } d = R_{\text{chip}} \sin 2\theta + l_p \cos 2\theta - HC \cos(2\theta - \gamma_0) - BH \sin(2\theta - \gamma_0)$$

$$= R_{\text{chip}} \sin 2\theta + l_p \cos 2\theta - H_{BC} \cos(2\theta - \gamma_0) - V_{BC} \sin(2\theta - \gamma_0)$$



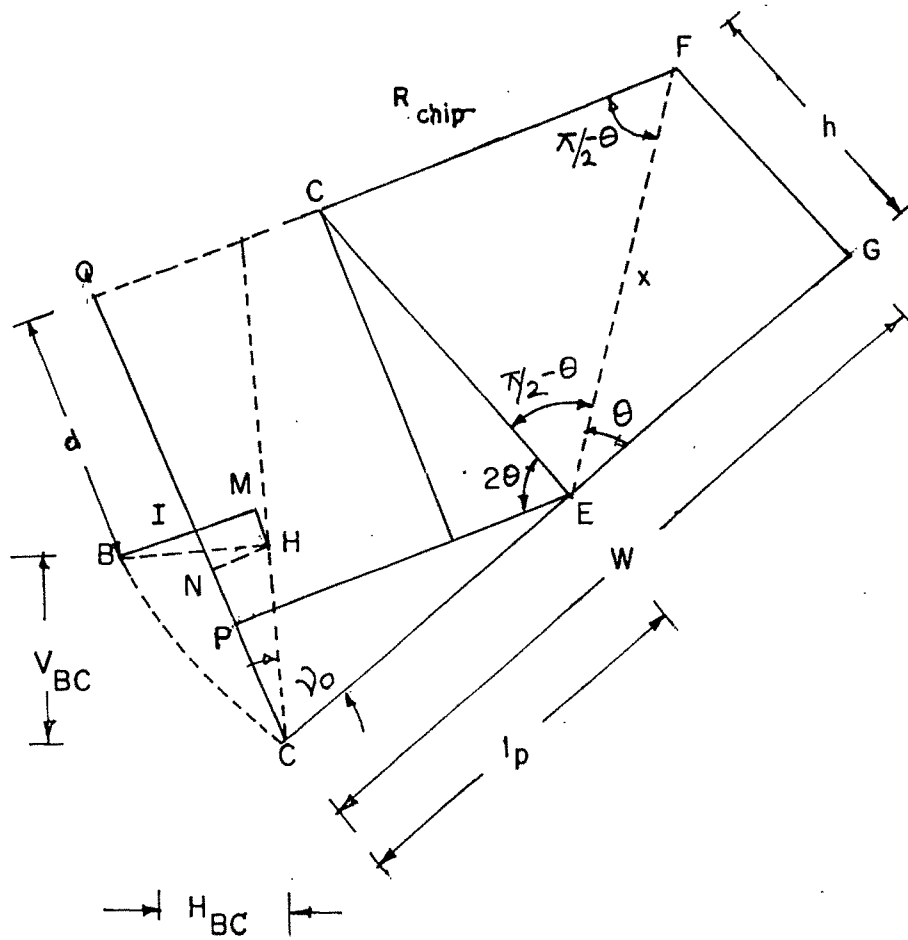


FIG. B.1 CONSTRUCTION FOR DETERMINING CURVATURE OF CHIP AND MOMENT ARM 'd'

APPENDIX-C

Procedure for deriving non-dimensional component of force

$$F_S = F_C \cos \beta - F_T \sin \beta \quad (C-1)$$

where, F_S , F_C and F_T are the shear force, tangential cutting force and thrust force respectively and β is the angle of shear.

$$\xi = t_1 / t_0$$

where t_1 = chip-thickness and t_0 = undeformed chip-thickness = $s \cdot \sin \phi_p$

$$\cot \beta = (\xi - \sin \gamma_0) / \cos \gamma_0 \quad (C-2)$$

where ξ is the cutting ratio and γ_0 is the rake angle.

For $\gamma_0 = 0$ and $\phi_p = \pi / 2$,

$$\cot \beta = \xi$$

$$\text{Now } F_S = k t_0 b / \sin \beta \quad (C-3)$$

where t_0 and b are undeformed chip-thickness and chip-width.

$$F_{NC} = F_C / F_S \sin \beta$$

$$F_{NT} = F_T / F_S \sin \beta \quad (C-4)$$

where F_{NC} and F_{NT} are the non-dimensional cutting force and thrust force respectively.

